# An ab Initio Molecular Orbital Study of the Thermal Decomposition of Fluorinated Monosilanes, SiH<sub>4-n</sub> $F_n$ (n = 0-4)

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The reactants, clusters, transition structures, and products for the various channels for the thermal decomposition of  $SiH_{4-n}F_n$ were optimized at the HF/6-31G\* level. The electron correlation contributions were calculated at MP4/6-31G\* and MP4/6-31G<sup>\*\*</sup> levels. In the decomposition of SiH<sub>4</sub>, SiH<sub>2</sub> + H<sub>2</sub> is favored over SiH<sub>3</sub> + H. For SiH<sub>3</sub>F, the SiHF + H<sub>2</sub> channel is preferred over SiH<sub>2</sub>F + H, SiH<sub>2</sub> + HF, and SiH<sub>3</sub> + F. In the decomposition of SiH<sub>2</sub>F<sub>2</sub>, the barrier for the formation of SiF<sub>2</sub> + H<sub>2</sub> is slightly lower than those of SiH<sub>2</sub> + H and SiHF + HF, while those of the SiH<sub>2</sub>F + F and SiH<sub>2</sub> + F<sub>2</sub> channels are considerably higher. For SiHF<sub>3</sub>, decomposition into SiF<sub>2</sub> + HF is favored with SiF<sub>3</sub> + H lying slightly higher. The other two channels  $SiHF_2 + F$  and  $SiHF + F_2$  are much higher in energy. In  $SiF_4$ , the decomposition into  $SiF_3 + F$  is favored over the reaction  $SiF_4 \rightarrow SiF_2 + F_2$ .

#### Introduction

The gas-phase stability of small silicon compounds is of considerable interest to the semiconductor industry, especially for processes such as chemical vapor deposition (CVD) of thin films and in etching of silicon surfaces.<sup>1-4</sup> In the chemical vapor deposition of amorphous silicon films, materials such as SiH<sub>4</sub>, Si<sub>2</sub>H<sub>6</sub>, SiF<sub>4</sub>, SiCl<sub>4</sub>, etc. or various mixtures of these are heated to 400-800 °C. Thermal decomposition of the starting materials is the initial step in the deposition. Previous theoretical studies have dealt with the thermal decomposition of  $SiH_4^1$  and  $Si_2H_6^2$ and the heats of formation of  $SiH_mF_n^{3-6}$  and  $SiH_mCl_n^{7}$ . The decomposition of  $SiH_{4-n}F_n$  is of interest since amorphous silicon films containing small percentages of fluorine have desirable electric properties for photovoltaic devices.8 In recent experimental work.<sup>9</sup> the rates for unimolecular decomposition of  $SiH_{4-n}F_n$ (n = 0, 1, 2) have been determined in the temperature range 1200-2000 K. The present paper outlines a theoretical study of the pathways, transition structures, and barriers for thermal decomposition of SiH<sub>4</sub>, SiH<sub>3</sub>F, SiH<sub>2</sub>F<sub>2</sub>, SiHF<sub>3</sub>, and SiF<sub>4</sub>. The following reactions have been considered:

$$SiH_4 \rightarrow SiH_2 + H_2$$
 (1)

$$SiH_4 \rightarrow SiH_3 + H$$
 (2)

$$SiH_3F \rightarrow SiHF + H_2$$
 (3)

$$SiH_3F \rightarrow SiH_2 + HF$$
 (4)

$$SiH_3F \rightarrow SiH_2F + H$$
 (5)

$$SiH_3F \rightarrow SiH_3 + F$$
 (6)

$$\mathrm{SiH}_2\mathrm{F}_2 \rightarrow \mathrm{SiF}_2 + \mathrm{H}_2 \tag{7}$$

$$SiH_2F_2 \rightarrow SiHF + HF$$
 (8)

$$SiH_2F_2 \rightarrow SiH_2 + F_2$$
 (9)

$$SiH_2F_2 \rightarrow SiHF_2 + H$$
 (10)

$$SiH_2F_2 \rightarrow SiH_2F + F$$
 (11)

$$SiHF_3 \rightarrow SiF_2 + HF$$
 (12)

- $SiHF_3 \rightarrow SiHF + F_2$ (13)
- $SiHF_3 \rightarrow SiF_3 + H$ (14)
- $SiHF_3 \rightarrow SiHF_2 + F$ (15)

$$SiF_4 \rightarrow SiF_2 + F_2$$
 (16)

$$SiF_4 \rightarrow SiF_3 + F$$
 (17)

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These reactions fall into two categories: (a) single bond dissociation (reactions 2, 5, 6, 10, 11, 14, 15, 17) and (b) decomposition into a silylene and a diatomic. The reverse of a single bond dissociation, i.e. simple radical-radical recombination, should have no activation barrier; hence the energy required for these decomposition pathways can be obtained from the heats of formation of the silanes and the silyl radicals. In our previous studies, 3,4 heats of formation were calculated for the various fluorinated silylenes, silvl radicals, and silanes. A reliable set of heats of formation was obtained using the isodesmic reactions

$$(a/n)\operatorname{SiH}_n + (b/n)\operatorname{SiF}_n \to \operatorname{SiH}_a F_b (a + b = n)$$
 (18)

$$(a/4)$$
SiF<sub>n</sub> +  $[(4 - a)/4]$ Si  $\rightarrow$  SiF<sub>a</sub> (a = 1, 2, 3) (19)

$$\operatorname{SiH}_{4-a}\operatorname{F}_a + \operatorname{SiH}_n \to \operatorname{SiH}_4 + \operatorname{SiF}_a(a = 1, 2, 3) \quad (20)$$

and combining the theoretical  $\Delta H$ 's calculated at the MP4SDTQ/6-31++G(2d,2p) level or better with the experimental  $\Delta H_{\rm f}^{\rm o}$  for SiH, and SiF<sub>4</sub>. Ho et al.<sup>6</sup> obtained similar results using the bond additivity approach and MP4/6-31G\*\* calculations. The second category of reactions is the reverse of the family of silylene insertions into H<sub>2</sub>, HF, and F<sub>2</sub> (reactions 1, 3, 4, 7-9, 12, 13, 16). The insertions of SiH<sub>2</sub>, SiHF, and SiF<sub>2</sub> into H<sub>2</sub> were studied in earlier work.<sup>10,11</sup> At the MP4SDQ/6-31G\*\* level, the barrier for insertion is 7.9 kcal/mol for SiH<sub>2</sub> + H<sub>2</sub>, 30.1 kcal/mol for SiHF + H<sub>2</sub>, and 61.1 kcal/mol for SiF<sub>2</sub> + H<sub>2</sub>. More extensive calculations on SiH<sub>2</sub> + H<sub>2</sub><sup>1</sup> lead to a barrier of 1.7 kcal/mol, in good agreement with recent experiments.<sup>12</sup> Of the other insertion reactions listed above, only SiH<sub>2</sub> + HF has been studied previously.13

In the present paper, transition structures and loose clusters are calculated for SiHF + HF, SiF<sub>2</sub> + HF, SiH<sub>2</sub> + F<sub>2</sub>, SiHF +

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Figure 1. Transition structures for SiH<sub>2</sub>, SiHF, and SiF<sub>2</sub> insertion into H<sub>2</sub>: no superscript, HF/3-21G optimized; asterisk, HF/6-31G\* optimized; double asterisk, MP2/6-31G\*\* optimized. Arrows indicate the HF/6-31G\* transition vectors.

 $F_2$ , and  $SiF_2 + F_2$ . These results are combined with previously computed barrier heights for silylene insertions and calculated heats of formation of  $\text{SiH}_n F_m$  (n + m = 2, 3, 4) to estimate the energetics of the various pathways for thermal decomposition of fluorine-substituted silanes.

#### **Computational Method**

Ab initio MO calculations were carried out with GAUSSIAN 88 and GAUSSIAN 9014 with split valence (3-21G)15 and polarization (6-31G\*, 6-31G\*\*)<sup>16</sup> basis sets. All geometries were fully optimized at the Hartree-Fock level with the 3-21G and 6-31G\* basis sets using analytical gradient methods; some structures were also optimized at the MP2/6-31G\* or MP2/6-31G\*\* levels. Vibrational frequencies and zero point energies were obtained at the HF/6-31G\* level using analytical second derivatives. Fourth order Møller-Plesset perturbation theory in the space of single. double, triple, and quadruple excitations (MP4SDTQ, frozen core) was used to estimate electron correlation energy. For some transition states, the reaction path was followed in internal coordinates<sup>17</sup> (nonmass weighted, step size = 0.4 au or rad) to confirm the mechanism of the reaction.

### **Results and Discussion**

The calculated total energies for the clusters and transition states for reactions 1-17 are given in Table I. The total energies for the reactants and products have been published previously.<sup>3,4</sup> The vibrational frequencies calculated at the HF/6-31G\* level are listed in Table II, and the optimized geometries for the transition state and clusters are given in Figures 1–7. Table III presents the calculated barriers for the silylene insertion reactions; Table IV shows the cluster well-depths. The computed thermal decomposition barriers are collected in Table V.

Geometries. SiXY + H<sub>2</sub>. The HF/3-21G, HF/6-31G\*, and MP2/6-31G\*\* optimized transition structures for  $SiH_4 \rightarrow SiH_2$ +  $H_2$  are shown in Figure 1a. The geometries are very similar and are characterized by a short  $SiH_2-H_2$  distance with the  $H_2$ in the symmetry plane. Replacing one or both of the silvlene hydrogens with fluorine does not change the configuration very much (Figure 1b,c). With F substitution, the H-H, Si-H, and Si-H<sub>2</sub> bonds tend to lengthen and the angles open up. Beyond the transition state,  $SiXY + H_2$  forms a weakly bound cluster



Figure 2. Clusters of SiH<sub>2</sub> and SiHF with H<sub>2</sub>: no superscript, HF/3-21G optimized; asterisk, HF/6-31G\* optimized.



Figure 3. Transition structures for SiH<sub>2</sub>, SiHF, and SiF<sub>2</sub> insertion into HF: no superscript, HF/3-21G optimized; asterisk, HF/6-31G\* optimized; double asterisk, MP2/6-31G\*\* optimized. Arrows indicate the HF/6-31G\* transition vectors.



Figure 4. Clusters of SiH<sub>2</sub>, SiHF, and SiF<sub>2</sub> with HF: no superscript, HF/3-21G optimized; asterisk, HF/6-31G\* optimized.

(Figure 2), characterized by a very long  $Si-H_2$  distance. The cluster is weakened by progressive F substitution to the extent that no stable cluster could be found for  $SiF_2 + H_2$ .<sup>3</sup>

SIXY + HF. The transition state for decomposition of SiHFXY into SiXY and HF (Figure 3a-c) is similar to that of SiH<sub>2</sub>XY  $\rightarrow$  SiXY + H<sub>2</sub>. The MP2-optimized transition state for SiH<sub>2</sub> +

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		6-31	G*		6-31G**					6-31G*
	HF	$E_2$	$E_3$	E <sub>4SDQ</sub>	HF	<i>E</i> <sub>2</sub>	<i>E</i> <sub>3</sub>	E <sub>4SDQ</sub>	E <sub>4T</sub>	ZPE
SiH₄	-291.22513	-0.081 89	-0.018 38	-0.004 70	-291.23084	-0.10815	-0.021 00	-0.004 26	-0.001 35	21.02
$SiH_2 + H_2$ (cl)	-291.12717	-0.08510	-0.022 20	-0.006 42	-291.13470	-0.107 78	-0.02371	-0.005 97	-0.001 13	15.93
$SiH_2 + H_2$ (ts)	-291.09765	-0.101 46	-0.02203	-0.00517	-291.10867	-0.12595	-0.023 07	-0.004 37	-0.00281	18.13
$SiH_2 + H_2$	-291.12661	-0.084 55	-0.02221	-0.006 48	-291.13396	-0.10707	-0.023 69	-0.006 03	0.001 09	14.58
$SiH_3 + H$	-291.104 36	-0.068 33	-0.01605	-0.004 24	-291.108 82	-0.08766	-0.01782	-0.003 80	-0.00116	14.35
SiH <sub>3</sub> F	-390.148 40	-0.251 30	-0.01083	-0.007 77	-390.15284	-0.271 35	-0.013 04	-0.007 68	-0.004 69	18.61
$SiHF + H_2$ (cl)	-390.059 04	-0.259 70	-0.01385	-0.010 49	-390.06513	-0.27575	-0.01486	-0.010 27	-0.005 28	13.20
$SiHF + H_2$ (ts)	-389.99693	-0.291 64	0.00477	-0.009 02	-390.007 06	-0.289 50	-0.01591	0.008 59	-0.006 29	15.40
SiHF + $H_2$	-390.05873	-0.259 49	-0.01385	-0.010 52	-390.06474	-0.275 44	-0.01485	-0.010 28	-0.005 26	12.44
$SiH_2 + HF$ (cl)	-390.013 51	-0.251 60	-0.01692	-0.007 88	-390.02493	-0.26913	-0.018 33	-0.007 65	-0.003 50	16.75
$SiH_2 + HF$ (ts)	-389.973 44	-0.277 48	-0.009 04	-0.010 47	-389.98211	-0.294 99	-0.010 34	-0.01043	-0.00815	15.17
$SiH_2 + HF$	-390.00269	-0.24595	-0.018 87	-0.007 54	-390.01418	-0.26371	-0.02003	-0.007 32	-0.003 38	14.17
$SiH_2F + H$	-390.021 07	-0.238 41	-0.008 11	-0.007 63	-390.02414	-0.247 90	0.013 00	-0.007 50	-0.004 69	11.99
$SiH_3 + F$	389.97108	-0.190 64	-0.024 47	-0.006 00	-389.975 54	-0.209 97	-0.026 24	-0.005 56	-0.002 36	14.35
SiH <sub>2</sub> F <sub>2</sub>	-489.08181	-0.42288	-0.003 57	-0.01094	-489.08483	-0.436 26	-0.00514	0.01099	-0.008 26	15.70
$SiF_2 + H_2$ (ts)	-488.90226	-0.443 04	-0.007 75	-0.01310	-488.911 37	-0.45441	-0.008 04	-0.01284	-0.01019	12.21
$SiF_2 + H_2$	-489.011 50	-0.436 06	-0.005 44	-0.01412	-489.01600	-0.44511	-0.005 79	-0.013 94	-0.009 61	9.86
SiHF + HF (cl)	-488.947 63	-0.42576	0.009 61	-0.009 69	-488.95763	-0.43681	-0.01011	-0.011 55	-0.008 02	14.28
SiHF + HF (ts)	-488.89964	-0.45048	-0.00112	-0.014 10	-488.906 90	-0.461 43	-0.001 88	-0.014 25	-0.01210	12.28
SiHF + HF	-488.93481	-0.42089	-0.010 51	-0.011 58	-488.94496	-0.432 08	-0.01119	-0.011 57	-0.007 55	12.03
$SiH_2 + F_2$ (cl)	-488.67915	-0.42260	-0.016 22	-0.01225	-488.68201	-0.43611	-0.017 35	-0.01198	-0.009 49	10.67
$SiH_2 + F_2$ (ts-syn)	-488.63584	-0.502 09	0.004 55	-0.01717	-488.63886	-0.51534	0.003 63	-0.016 24	-0.029 84	11.84
$SiH_2 + F_2$ (ts-anti)	488.65992	-0.484 43	0.001 87	-0.01716	-488.66282	0.497 83	0.00075	-0.01661	-0.023 76	11.69
$SiH_2 + F_2$	-488.677 54	-0.419 99	-0.01690	-0.02005	-488.680 39	-0.433 46	-0.018 03	-0.01172	-0.00915	9.72
SiHF, + H	-488.94906	-0.410 30	-0.000 36	-0.01103	-488.95061	-0.41673	-0.001 04	-0.011 01	-0.008 40	9.06
$SiH_2F + F$	-488.88779	-0.36072	-0.016 53	0.009 39	-488.89086	-0.370 21	-0.021 42	-0.009 26	-0.005 89	11.99
SiHF,	-588.018 33	-0.594 58	0.00317	-0.01387	-588.01985	-0.60115	0.002 36	-0.01393	-0.011 85	12.28
$SiF_2 + HF$ (cl)	-587.898 38	-0.601 08	-0.001 42	-0.01511	-587.90690	-0.60518	-0.001 45	-0.01516	-0.012 20	10.98
$SiF_2 + HF$ (ts)	-587.837 00	-0.624 76	-0.00676	-0.017 41	-587.84244	-0.628 89	0.006 68	-0.017 60	-0.016 21	8.90
$SiF_2 + HF$	-587.887 58	-0.597 46	-0.00210	-0.01518	-587.896 22	-0.601 75	-0.00213	-0.01523	-0.011 90	9.45
$SiHF + F_2$ (cl)	-587.61096	-0.55969	-0.008 08	-0.016 25	-587.61247	-0.603 88	-0.008 73	-0.01616	-0.013 57	8.42
$SiHF + F_2$ (ts-syn)	-587.55568	-0.690 36	0.013 57	-0.018 83	-587.557 40	-0.696 88	0.013 31	-0.01793	-0.037 44	8.58
SiHF + $F_2$ (ts-anti)	-587.585 54	-0.664 44	0.01064	-0.02061	-587.587 04	-0.67119	0.01004	-0.020 27	-0.029 64	8.66
SiHF + $F_2$	-587.60966	-0.594 93	-0.008 54	-0.024 09	-587.61117	-0.601 83	-0.009 19	-0.01597	-0.013 32	7.58
$SiF_3 + H$	-587.87947	-0.581 60	0.006 97	-0.01401	-587.879 47	-0.581 60	0.006 97	-0.014 01	-0.01206	5.76
$SiHF_{2} + F$	-587.81578	-0.53261	-0.008 78	0.012 79	-587.81733	-0.53904	-0.009 46	-0.01277	-0.009 60	9.06
SiF₄	-686.949 84	-0.76461	0.00917	-0.016 37	-686.949 84	-0.76461	0.00917	-0.016 37	-0.015 35	8.49
$SiF_{2} + F_{2}$ (cl)	-686.563 50	-0.773 29	0.000 24	-0.01980	-686.563 50	-0.773 29	0.000 24	-0.019 80	-0.01784	5.26
$SiF_{2} + F_{2}$ (ts-anti)	686.522 22	-0.86001	0.019 90	-0.019 29	-686.52222	-0.86001	0.01990	-0.019 29	-0.038 50	5.42
$SiF_2 + F_2$	-686.56243	-0.771 50	-0.00013	-0.027 69	-686.56243	-0.771 50	-0.00013	-0.01963	-0.01767	5.00
$SiF_3 + F$	-686.74619	-0.703 91	-0.001 45	-0.01577	-686.74619	-0.703 91	-0.001 45	-0.01577	-0.013 26	5.76

<sup>a</sup> Total energies in atomic units; zero point energies in kcal/mol.

#### TABLE II: Frequencies<sup>a</sup>

molecule	frequencies
	Transition States
SiH <sub>2</sub> H <sub>2</sub>	1630i, 837, 863, 1027, 1125, 1782, 2263, 2382, 2400
SiHFH2	1786i, 671, 762, 887, 923, 1146, 1635, 2312, 2436
SiF <sub>2</sub> H <sub>2</sub>	1993i, 342, 612, 761, 926, 995, 1034, 1473, 2397
SiHFHF	1860i, 227, 516, 714, 815, 939, 990, 2027, 2366
SiF <sub>2</sub> HF	1863i, 208, 279, 390, 661, 699, 957, 1007, 2028
SiH <sub>2</sub> HF	1886i, 497, 619, 778, 880, 1095, 2020, 2359, 2360
$SiH_2 - F_2$ (syn)	1036i, 221, 256, 607, 733, 845, 1016, 2290, 2318
$SiH_2 - F_2$ (anti)	748i, 185, 285, 579, 630, 813, 1089, 2294, 2304
$SiHF-F_2$ (syn)	963i, 126, 241, 303, 609, 719, 857, 939, 2210
SiHFF <sub>2</sub> (anti)	729i, 111, 193, 289, 575, 749, 916, 954, 2276
$SiF_2 - F_2$ (anti)	648i, 102, 103, 285, 325, 431, 593, 951, 1004
	Clusters
SiH2H2	90, 95, 209, 236, 345, 1129, 2208, 2219, 4611
SiHFH <sub>2</sub>	31, 69, 79, 133, 234, 921, 964, 2169, 4632
$SiH_2 - F_2$	46, 47, 73, 213, 285, 1131, 1241, 2210, 2220
SiHFF2	33, 62, 103, 105, 351, 919, 968, 1288, 2059
SiHFHF	132, 194, 332, 504, 570, 867, 966, 2181, 4243
SiF <sub>2</sub> HF	88, 135, 179, 284, 374, 522, 894, 934, 4271
SiH <sub>2</sub> HF	157, 167, 419, 478, 646, 1120, 2220, 2230, 4283
$SiF_2 - F_2$	7, 22, 40, 53, 55, 373, 932, 948, 1243

<sup>a</sup> In cm<sup>-1</sup> at the HF/6-31G<sup>\*</sup> level.

HF differs little from the Hartree-Fock-optimized geometry, suggesting the  $HF/6-31G^*$  level is adequate for the fluorinesubstituted cases. The Si-F distance in SiXY--HF decreases with F substitution while the Si-H distance remains the same. The transition vectors for insertion are dominated by the motion of



Figure 5. Transition structures for SiH<sub>2</sub>, SiHF, and SiF<sub>2</sub> insertion into  $F_2$  via the syn approach: no superscript, HF/3-21G optimized; asterisk, HF/6-31G\* optimized. The MP2/6-31G\*-optimized structure for SiH<sub>2</sub> +  $F_2$  (double asterisk) is a second-order saddle point; all other structures are first-order saddle points.

the hydrogen and, hence, could be described equally well as a 1,2 hydrogen shift across the Si-F bond. The clusters (Figure 4a-c) are characterized by relatively short Si-F distances associated with the lone pair on the F interacting with the empty  $p_{\tau}$  orbital of silylene. With F substitution of the silylene, the Si-F distance in the cluster lengthens, suggesting a progressive weakening of the interaction. However, this is balanced by an interaction between the HF and SiF bond dipoles as indicated by the alignment of these bonds in SiHF--HF and SiF<sub>2</sub>--HF.

SiXY +  $F_2$ . At the Hartree-Fock level, two families of transition structures can be found for silylene insertion into  $F_2$ : one

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#### TABLE III: Barriers for Silylene-Insertion Reactions<sup>a</sup>

		6-3	1 <b>G*</b>				6-31G**			HF/ 6-31G*	
reactions	HF	MP2	MP3	MP4	HF	MP2	MP3	MP4 <sup>b</sup>	MP4 <sup>c</sup>	ΔΖΡΕ	
$SiH_2 + H_2 \rightarrow SiH_4$	21.7	11.1	11.2	12.0	19.4	7.6	8.0	9.0	7.9	3.5	
$SiHF + H_2 \rightarrow SiH_3F$	41.7	21.6	33.3	34.2	39.2	30.3	29.7	30.7	30.1	3.0	
$SiF_2 + H_2 \rightarrow SiH_2F_2$	70.9	66.5	65.1	65.7	68.0	62.2	60.8	61.5	61.1	2.3	
$SiH_2 + HF \rightarrow SiH_3F$	19.4	-0.04	5.7	3.9	21.1	1.5	7.6	5.6	2.6	1.0	
$SiHF + HF \rightarrow SiH_2F_2$	22.1	3.5	9.4	7.8	23.9	5.5	11.3	9.6	6.8	0.3	
$SiF_2 + HF \rightarrow SiHF_3$	31.2	14.1	19.6	18.2	33.2	16.2	21.7	20.2	17.5	-0.6	
$SiH_2 + F_2 \rightarrow SiH_2F_2$ (syn)	28.3	-23.2	-9.8	-8.0	28.2	-23.2	-9.6	-12.4	-25.4	2.1	
(anti)	13.0	-27.4	-15.6	-13.8	13.0	-27.4	-15.6	-18.7	-27.8	2.0	
$SiHF + F_2 \rightarrow SiHF_3$ (syn)	34.9	-25.0	-11.4	-13.0	34.7	-24.9	-10.7	-12.0	-27.3	1.0	
(anti)	16.2	-27.4	-15.4	-13.2	16.2	-27.3	-15.2	-17.9	-28.2	1.1	
$SiF_2 + F_2 \rightarrow SiF_4$ (anti)	25.7	-29.9	-17.3	-12.0	25.7	-29.9	-17.3	-17.1	-30.2	0.4	

 ${}^{a}\Delta E$  in kcal/mol, with  $\Delta ZPE$  included, using the HF/6-31G\*-optimized geometry.  ${}^{b}$  Including single, double, and quadrupole excitations.  ${}^{c}$  Including single, double, triple, and quadrupole excitations.

TABLE I	V:	Cluster	W	ell	-De	ptl	1S
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	6-31G*			6-31G**					HF/ 6-316*		
reaction	HF	MP2	MP3	MP4 <sup>b</sup>	HF	MP2	MP3	MP4 <sup>b</sup>	MP4 <sup>c</sup>	ΔΖΡΕ	
$SiH_2 - H_2 \rightarrow SiH_2 + H_2$	0.4	0.7	0.7	0.6	0.5	0.9	0.9	0.9	0.9	-1.4	
$SiHF - H_2 \rightarrow SiHF + H_2$	0.2	0.3	0.3	0.3	0.2	0.4	0.4	0.4	0.4	-0.8	
$SiH_{2} - HF \rightarrow SiH_{2} + HF$	6.8	10.3	9.1	9.3	6.8	10.2	9.0	9.2	9.2	-2.6	
SiHFHF → SiHF + HF	8.1	11.1	10.4	7.5	8.0	10.9	10.2	10.2	10.5	-2.3	
$SiF_{2} - HF \rightarrow SiF_{2} + HF$	6.8	9.0	8.6	8.6	6.7	8.9	8.4	8.4	8.6	-1.5	
$SiH_{2} - F_{2} \rightarrow SiH_{2} + F_{2}$	1.0	2.6	2.2	2.4	1.0	2.7	2.3	2.4	2.6	-1.0	
SiHFF, → SiHF + F,	3.6	0.8	2.1	1.8	0.8	2.1	1.8	1.9	2.1	-1.0	
$SiF_2 - F_2 \rightarrow SiF_2 + F_2$	0.7	1.8	1.5	1.6	0.7	1.8	1.5	1.6	1.8	-0.3	

 $^{a}\Delta E$  in kcal/mol, with  $\Delta ZPE$  not included, using the HF/6-31G\* optimized geometry.  $^{b}$  Including single, double, and quadruple excitations.  $^{c}$  Including single, double, triple and quadruple excitations.

with the migrating F syn to the silylene lone pair (Figure 5a-c) and the other with the F anti to the lone pair (Figure 6a-c). The latter is consistently lower in energy at the Hartree-Fock level. For both the syn and anti transition structures, the  $Si-F_2$  bond is shorter than that in the corresponding SiXY + HF transition state. Fluorine substitution tends to shorten the Si-F bond and lengthen the F-Fbond. The syn transition state for  $SiF_2 + F_2$  does not exist at the HF/6-31G\* level; instead the optimization stepped monotonically to the anti conformer. Reaction path following<sup>17</sup> confirmed that the syn transition state proceeds to the fluorosilane product by the anticipated migration of the fluorine to the silylene lone pair. However, reaction path following showed that the anti transition structure reached the products by a backside attack on the lone pair with concomitant inversion of the silicon. Optimization of the syn transition state for  $SiH_2 + F_2$  at the MP2/ 6-31G\* level yields a structure that is significantly earlier on the reaction coordinate for insertion (Figure 5a). However, this structure is a second-order saddle point. The MP2 optimization and reaction path following for the anti approach revealed that insertion occurs without a barrier and proceeds to an intermediate that is ca. 80 kcal/mol more stable than the reactants (Figure 6a, similar in energy and structure to  $SiH_2F + F$ ). This structure does not exist on the Hartree-Fock surface (optimization at the HF level starting from this structure leads directly to products). The unusual behavior of the HF and MP2 surfaces for  $SiH_2$  +  $F_2$  is, no doubt, related to the difficulty in treating the  $F_2$  bond at simple levels of theory. Because  $SiXY + F_2 \rightarrow SiXYF_2$  reactions are very exothermic (ca. 230-250 kcal/mol) and the  $F_2$ bond is relatively weak (37 kcal/mol), these reactions may occur stepwise with F atom transfer to form SiXYF followed by radical recombination to form SiXYF<sub>2</sub>. The possibility of a radicaloid mechanism is supported to some extent by the fact that the RHF-optimized transition state has a substantial UHF instability. The energy surface for  $SiH_2 + F_2$  is being studied with higher levels of theory and larger basis sets.<sup>18</sup> Since the F<sub>2</sub>-elimination



Figure 6. Transition structures for SiH<sub>2</sub>, SiHF, and SiF<sub>2</sub> insertion into  $F_2$  via the anti approach: no superscript, HF/3-21G optimized; asterisk, HF/6-31G\* optimized. All structures are first-order saddle points except the MP2/6-31G\*-optimized structure for SiH<sub>2</sub> +  $F_2$  (double asterisk) which is a stable intermediate. On the MP2/6-31G\* surface, the SiH<sub>2</sub> +  $F_2$  reaction occurs without a barrier and proceeds to this low-energy intermediate.

channels for  $SiH_{4-n}F_n$  lie 80–160 kcal/mol above the lowest energy pathways (see below), the uncertainties in the surfaces for SiXY +  $F_2$  do not affect the mechanism for thermal decomposition.

The long-range clusters are shown in Figure 7a-c. The Si-F distances in SiXY +  $F_2$  are longer than those in SiXY + HF and increase progressively with fluorine substitution, though not as much as the Si-H distances in SiXY +  $H_2$ .

**Energetics.** A previous study of the insertion of SiH<sub>2</sub>, SiHF, and SiF<sub>2</sub> into H<sub>2</sub> found that there is a very large increase in the insertion barrier with fluorine substitution,<sup>10</sup> about 30 kcal/mol per fluorine as shown in Table III. For SiH<sub>2</sub> + H<sub>2</sub>, the 7.9 kcal/mol barrier is reduced to 3.6 kcal/mol at the MP4/6-31+ G(2df,p) level using the MP2/6-31G\*\*-optimized geometry; more extensive calculations<sup>1</sup> lowered the barrier to 1.7 kcal/mol. The most recent analysis of the experimental data<sup>12</sup> yielded an activation energy of 0.5 kcal/mol; this suggest that the MP4/6-31G\*\*

<sup>(18)</sup> Ayala, P. Y.; Ignacio, E. W.; Schlegel, H. B. Manuscript in preparation.



Figure 7. Clusters of SiH<sub>2</sub>, SiHF, and SiF<sub>2</sub> with  $F_2$ : no superscript, HF/3-21G optimized; asterisk, HF/6-31G\* optimized.

TABLE V: Thermal Decomposition Barriers of  $SiH_nF_{4-n}^a$ 

reaction	$\Delta H_{\rm r}(0)$	forward barrier	reverse barrier
SiH4			<u> </u>
$\rightarrow$ SiH <sub>2</sub> + H <sub>2</sub>	55	57	2
$\rightarrow$ SiH <sub>3</sub> + H	89	89	0
SiH <sub>4</sub> F			
$\rightarrow$ SiHF + H <sub>2</sub>	46	70	24
→ SiH <sub>2</sub> + HF	84	91	7
$\rightarrow$ SiH <sub>2</sub> F + H	92	92	0
$\rightarrow$ SiH <sub>3</sub> + F	150	150	0
SiH <sub>2</sub> F <sub>2</sub>			
$\rightarrow$ SiF <sub>2</sub> + H <sub>2</sub>	31	86	55
→ SiHF + HF	82	93	11
$\rightarrow$ SiHF, + H	94	94	0
→ SiH <sub>2</sub> F + F	159	159	0
$\rightarrow$ SiH <sub>2</sub> + F,	250	≥250	≥0
SiHF <sub>3</sub>			
$\rightarrow$ SiF, + HF	68	89	21
$\rightarrow$ SiF <sub>3</sub> + H	98	98	0
→ SiHF, + F	163	163	0
$\rightarrow$ SiHF + F <sub>2</sub>	249	≥249	≥0
SiF₄			
$\rightarrow$ SiF <sub>1</sub> + F	163	163	0
$\rightarrow$ SiF <sub>2</sub> + F <sub>2</sub>	232	≥232	≥0
<b>41</b> 1 1 / 1			

<sup>*a*</sup> In kcal/mol.

values are too high by ca. 6 kcal/mol. The SiXY + H<sub>2</sub> barriers listed in Table V are calculated using isodesmic reaction 21 at the MP4SDTQ/6-31G\*\* level combined with the best available theoretical value for SiH<sub>2</sub> + H<sub>2</sub>  $\rightarrow$  SiH<sub>2</sub>-H<sub>2</sub> (ts) (1.7 kcal/mol).

For SiH<sub>2</sub>, SiHF, and SiF<sub>2</sub> insertion into HF, the barriers are small and the increase in barrier on F substitution on the silylene is much less than that for insertion into H<sub>2</sub>, about 5-10 kcal/mol per F. For SiH<sub>2</sub> + HF, higher level calculations (MP4/6-31+ G(2df,p)) using the MP2/6-31G\*\*-optimized geometry give an insertion barrier of 6.6 kcal/mol. This suggests a systematic error of ca. +4 kcal/mol. Similar to the SiXY + H<sub>2</sub> insertion barriers, the barriers for insertion into HF listed in Table V have been computed using isodesmic reaction 22 at the MP4/6-31G\*\* level



Figure 8. Potential energy profiles for the various channels for the thermal decomposition of  $SiH_4$ ,  $SiH_3F$ ,  $SiH_2F_2$ , and  $SiHF_3$ .

combined with a value of 6.6 kcal/mol for SiH<sub>2</sub> + HF  $\rightarrow$  Si-H<sub>2</sub>-HF (ts) obtained from the higher level calculations.

SiXY<sub>2</sub> + HF + SiH<sub>2</sub>-HF (ts) 
$$\rightarrow$$
  
SiXY<sub>2</sub>-HF (ts) + SiH<sub>2</sub> + HF (X, Y = H, F) (22)

At the Hartree-Fock level, the barrier for SiXY insertion into  $F_2$  is 15-20 kcal/mol lower for the anti transition state than for the syn. With fluorine substitution, the barrier increases by ca. 5 kcal/mol per fluorine. When correlation corrections are computed at the Hartree-Fock-optimized geometries, the barriers change drastically (dropping by 30-50 kcal/mol); this is due to the dramatic differences between the HF and MP2 potential energy surfaces and optimized geometries discussed above. The MP2/6-31G\* optimizations and reaction path following indicate that there is no barrier for SiH<sub>2</sub> insertion into  $F_2$ . Even in the absence of a barrier for insertion, the SiXY +  $F_2$  decomposition channel is disfavored by 80-160 kcal/mol compared to other pathways.

The cluster well-depths are listed in Table IV. The clusters between the silylenes and  $H_2$  are weakly bound (<1 kcal/mol), and the binding energy decreases with fluorine substitution of the silylenes. The clusters with HF are more strongly bound (ca. 10 kcal/mol), reflecting the donation of the fluorine lone pair into the empty  $p_{\pi}$  orbital of the silvlene as well as the dipole-dipole interaction. The well-depth for the clusters with  $F_2$  are intermediate between those of  $H_2$  and HF.

Figure 8a shows the thermal decomposition of SiH<sub>4</sub> to SiH<sub>2</sub> +  $H_2$  as the preferred path with a barrier of ca. 57 kcal/mol. The  $SiH_3$  + H channel is higher by about 30 kcal/mol. Figure 8b shows the four lowest energy pathways for the SiH<sub>3</sub>F decomposition. The SiHF +  $H_2$  channel is the favored, with a barrier of 70 kcal/mol; the SiH<sub>2</sub> + HF and SiH<sub>2</sub>F + H paths lie ca. 20 kcal/mol higher, with barriers of 91 and 92 kcal/mol, respectively. The SiH<sub>3</sub> + F channel is 150 kcal/mol above that of SiH<sub>3</sub>F. For the decomposition of  $SiH_2F_2$  (Figure 8c), there are three closely competing channels,  $SiF_2 + H_2$ , SiHF + HF, and  $SiHF_2 + H$ , each with barriers of ca. 90 kcal/mol. The other two channels,  $SiH_2F + F$  and  $SiH_2 + F_2$ , are very much higher in energy, with barriers 159 and ≥250 kcal/mol, respectively. Elimination of HF is the preferred pathway for SiHF<sub>3</sub>, with Si-H bond cleavage being 9 kcal/mol higher (Figure 8d). For  $SiF_4$  decomposition, breaking a single SiF is overwhelmingly favored over  $F_2$  elimination.

The thermal decompositions of SiH<sub>4</sub>, SiH<sub>3</sub>F, and SiH<sub>2</sub>F<sub>2</sub> diluted

in Ar have been studied by shock tube methods.<sup>9</sup> The temperature and pressure dependences of the reaction rates have been fitted using Troe's approach. The threshold obtained for  $SiH_4$  (59 kcal/mol) agrees well with the calculated barrier (57 kcal/mol<sup>1</sup>). The  $E_0$  for SiH<sub>3</sub>F decomposition (62 kcal/mol) is consistent with the heat of reaction for the SiHF + H<sub>2</sub> channel ( $\Delta H_r = 46$ kcal/mol) but not for the SiH<sub>2</sub> + HF channel ( $\Delta H_r = 84$ kcal/mol). However, the  $E_0$  from the fit of the experimental data (62 kcal/mol) is lower than the calculated barrier (70 kcal/mol), suggesting the latter is overestimated by 8 kcal/mol. For  $SiH_2F_2$ , the fitting yields  $E_0 = 72$  kcal/mol, ruling out the SiHF + HF and SiHF<sub>2</sub> + H channels ( $\Delta H_r = 84$  and 94 kcal/mol, respectively) and suggests the theoretical barrier for  $SiH_2F_2 \rightarrow SiF_2 +$ H<sub>2</sub> (86 kcal/mol) is overestimated by 14 kcal/mol. However, because the experimental data is far from the high-pressure limit and spans a narrow range of pressures, some caution is required in interpreting the results.

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Registry No. SiH<sub>4</sub>, 7803-62-5; SiH<sub>3</sub>F, 13537-33-2; SiH<sub>2</sub>F<sub>2</sub>, 13824-36-7; SiHF<sub>3</sub>, 13465-71-9; SiF<sub>4</sub>, 7783-61-1.

## Spin Potential in Kohn–Sham Theory

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The spin potential, a recently defined quantity (Galván, M.; Vela, A.; Gázquez, J. L. J. Phys. Chem. 1988, 92, 6470), is obtained for atoms from Z = 3 to Z = 54 within the framework of spin-polarized Kohn-Sham theory in the local density approximation. It is shown that this quantity has periodic behavior such as the electronegativity or ionization potential. A relationship between spin potential and processes in which the system changes its multiplicity at a constant number of electrons is established. This relationship is used to calculate pairing energies. Then, spin potential emerges as a measure of the tendency of a system to change its spin polarization.

### Introduction

One of the most encouraging features of density functional theory  $(DFT)^1$  is that it has given a framework to rationalize such concepts as electronegativity<sup>2</sup> and hardness and softness,<sup>3</sup> and it has also motivated the definition of new quantities that have been proven to be useful as reactivity criteria (i.e., the Fukui function<sup>4</sup> and local softness and local hardness<sup>5</sup>).

On the other hand, it is well-known that the spin-polarized version of DFT improves the description of electronic structure of atoms, molecules, and solids.<sup>6</sup> Besides quantities such as electronegativity, hardness, and the Fukui function, some new global and local parameters appear in this theory: the generalized Fukui functions and hardnesses and the spin potential.<sup>7</sup> Within this theory, the energy functional in the absence of a magnetic field is expressed in the form<sup>8,9</sup>

$$E[\rho,\rho_{\rm s},\vartheta(\mathbf{r})] = F[\rho,\rho_{\rm s}] + \int \vartheta(\mathbf{r}) \ \rho(\mathbf{r}) \ \mathrm{d}\mathbf{r} \qquad (1)$$

where  $\rho(\mathbf{r}) = \rho_{\uparrow}(\mathbf{r}) + \rho_{\downarrow}(\mathbf{r})$  is the total charge density,  $\rho_{s}(\mathbf{r}) = \rho_{\uparrow}(\mathbf{r})$  $-\rho_{\downarrow}(\mathbf{r})$  is the spin density, and  $\vartheta(\mathbf{r})$  is the external potential. In this formalism, the charge and spin distributions are independent variables; thus there are two Euler equations associated with the

energy-minimization process:7

$$\mu_N = \left(\frac{\delta E}{\delta \rho(\mathbf{r})}\right)_{\rho_v,\vartheta(\mathbf{r})} = \vartheta(\mathbf{r}) + \frac{\delta F}{\delta \rho(\mathbf{r})}$$
(2)

$$\mu_{\rm s} = \left(\frac{\delta E}{\delta \rho_{\rm s}({\bf r})}\right)_{\rho,\vartheta({\bf r})} = \frac{\delta F}{\delta \rho_{\rm s}({\bf r})} \tag{3}$$

 $\mu_N$  and  $\mu_s$  are, respectively, the Lagrange multipliers associated with the restrictions

$$\int \rho(\mathbf{r}) \, \mathrm{d}\mathbf{r} = N = N_{\uparrow} + N_{\downarrow} \tag{4}$$

$$\int \rho_{\rm s}(\mathbf{r}) \, \mathrm{d}\mathbf{r} = N_{\rm s} = N_{\uparrow} - N_{\downarrow} \tag{5}$$

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